# Forecasting US Army enlistment contract production in complex geographical marketing areas

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### Abstract

**Purpose**—The purpose of this paper is to demonstrate an improved method for forecasting the US Army recruiting. **Design/methodology/approach** — Time series methods, regression modeling, principle components and marketing research are included in this paper.

**Findings** – This paper found the unique ability of multiple statistical methods applied to a forecasting context to consider the effects of inputs that are controlled to some degree by a decision maker.

**Research limitations/implications** – This work will successfully inform the US Army recruiting leadership on how this improved methodology will improve their recruitment process.

Practical implications - Improved US Army analytical technique for forecasting recruiting goals ...

**Originality/value** – This work culls data from open sources, using a zip-code-based classification method to develop more comprehensive forecasting methods with which US Army recruiting leaders can better establish recruiting goals.

Keywords Regression, Comparative studies, Sales forecasting

Paper type Research paper

The authors are indebted to the USAREC – specifically the Marketing & Mission Analysis Division – for their supply of data and willingness to let us aid their decision-making process.

Complex geographical marketing areas

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Received 9 March 2017 Revised 26 June 2017 Accepted 15 August 2017



Journal of Defense Analytics and Logistics Vol. 1 No. 1, 2017 pp. 69-87 Emerald Publishing Limited 2399-6439 DOI 10.1108/JDAL-03-2017-0001

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## IDAL Introduction

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Since the formal elimination of the draft by Congress in 1973, the USA Army has maintained an All-Volunteer Force (AVF) (Waddell, 2005, pp. 413-442). At the lowest echelon of the Army recruiting system, US Army Recruiters are tasked to help fill the ranks of the AVF by actively pursuing qualified future soldiers with the ultimate goal of generating required enlistments. At higher echelons of recruiting leadership, however, a fundamental concern arises in how best to distribute recruiting goals to subordinate recruiting echelons throughout the country.

Implied in the latter concern is an assumption that a quantitative relationship between numerous recruiting factors – both within and outside of the recruiters' control – and enlistment production in each geographical recruiting area exits, can be satisfactorily established and can be exploited for forecasting purposes. If so, recruiting leadership can then maximize potential recruiting contracts by altering recruiting goals subject to a set of organizational constraints. Thus, the two primary steps of setting recruiting goals consist of:

- defining an appropriate quantitative relationship that is robust to extrapolation into the future; and
- maximizing the outputs based on organizational constraints and the quantitative model parameters found in the first step. We use the acronym US Army Recruiting Command (USAREC) to refer to the corporate, goal-setting body of Army recruiting leadership.

This article focuses on the first of recruiting leadership's tasks – the development of a quantitative relationship between recruiting market factors and enlistment production – as it is fundamental to successful execution of the second task, optimizing production. We are not the first to do this; USAREC has used and currently uses such quantitative models in the past. We do however offer an improved methodology for achieving a useful quantitative model.

We first establish the extent to which we can accurately forecast the relationship between enlistment supply and demand factors and enlistment contract production. We assume as supply factors those which are outside of the recruiters' control; local unemployment rates are an example. Enlistment demand factors, by contrast, are those over which the Army and recruiters have some control; numbers of recruiters on-hand and recruiting goals are examples. In terms of the response, we focus specifically on Regular Army (RA) enlistment contracts in 38 recruiting regions that span the USA, territories excluded. We subdivide the enlistment contracts into three mutually exclusive categories of interest to USAREC:

- (1) high-aptitude high school graduates (GA);
- (2) high-aptitude high school seniors (SA); and
- (3) all others (OTH) (Flesichmann and Nelson, 2014).

These are not the standard responses used by USAREC in their forecasting model, but we address in this paper why changing to these make sense.

We analyze data from both recruiting organizations and open sources for the period Fiscal Year (FY) 2010-2014. We take advantage of open source data at the county level and map this county-level data to each ZIP code-based recruiting market boundary. To complete this mapping, we introduce a way to compress data from over 3,000 counties and 42,000 ZIP Codes into 38 markets. We then apply principal components analysis (PCA) and mixed

stepwise regression to the re-mapped data to develop adequate, parsimonious models for each recruiting market and contract type. The application of PCA represents a significant contribution to the level of statistical rigor in our model development methodology over previous efforts.

Quantitative prediction models are useful when they yield accurate predictions. We use hold-out samples for model validation. We use only the first 75 per cent of the data to estimate ordinary least squares models; the latter 25 per cent of the data are used in forecast validation. To obtain a better appraisal of model stability during validation, we create additional realism by using simple linear trend forecasts of market supply variables. At the conclusion of this step, we achieve our penultimate objective by rendering quantitative market- and contract-specific comparisons of model performance within the context of a forecasting scenario. As a brief concluding excursion, we compare our multivariate forecasting approach to several univariate time series models.

In summary, we introduce an improved methodology for model development and assessment. To this end, we introduce an improved way to generate appropriate response data, and we demonstrate the use of principle components analysis to reduce model dimensionality and demonstrate an improved level of statistical rigor in our model development methodology. We also present an empirical study comparing our model to other common models.

#### Background

There is a vast literature on military recruitment, enlistment and retention. We focus on macro- and micro-economic studies. Macroeconomic studies are highly aggregated geographically, involving only a handful of national regions. Microeconomic studies are geographically disaggregated, typically at the ZIP code level. Due to space limitations, we here provide general findings based on a detailed discussion found in McDonald (2016).

Our review of pertinent literature on Armed Forces recruiting spans a 26-year period from 1985 through 2011. In total, macroeconomic studies of enlistment supply are helpful in describing the "big picture" of recruiting models. There seems to be some general agreement between these studies in the significance of a few select factors: unemployment, qualified military available population, veteran population and recruiter strength are of particular importance in this regard (Asch *et al.*, 2009; Warner *et al.*, 2001; Dertouzos and Garber, 2006, 2008; Dertouzos, 1985). However, these works have limited capacity to predict contract production for geographical areas corresponding to recruiting market boundaries. We therefore acknowledge the added value of microeconomic models in both their geographic specificity and use of validation data despite their reduced specificity in the response and difficulties in comparing fit adequacy (Gibson *et al.*, 2011, 2009).

There are useful conclusions derived from the prior literature. First, the literature is dominated by econometric methodology. The econometric studies share a common objective of describing socioeconomic effects on recruiting over time. In nearly every study, this involved some form of regression. We use a similar quantitative modeling methodology albeit with useful extensions.

Second, there is some broad agreement that several factors are correlated with recruit production. Of these, geography appears to be statistically significant (Dertouzos and Garber, 2006, 2008). Unfortunately, we cannot conclude how non-geographic factor effects change with respect to geographic location; each study uses different geographic boundary definitions, none of which correspond to actual USAREC definitions. In any case, geography is statistically significant based on the total body of empirical results. We do note with some caution that statistics gathered at the microeconomic level may have greater measurement

Complex geographical marketing areas error (Murray and McDonald, 1999). Thus, our methodology seeks an appropriate balance between required geographic specificity with respect to recruiting markets and data measurement errors inherent in higher resolution. We maintain a variable set broadly consistent with previous literature to provide a general basis for comparison.

Interestingly, relatively little of the previous research specifies predictive models designed to produce forecasts into future time periods. Recruiting – like any private-sector marketing effort—requires decision-making (i.e. an irrevocable allocation of resources) in the face of uncertainty (Howard and Abbas, 2015, pp. 1-19). While the studies we reviewed provided some indication of how variables respond to time, most did not explicitly describe model performance in an out-of-sample time period or provide any kind of probabilistic statement regarding future behavior. This observation is a primary motivator for our methodology, specifically with regard to our model validation efforts.

#### Methodology

#### Data description and cleaning

We collected data from USAREC and open sources. Our goals were to use variables mentioned in previous literature and provide a representative sample of pertinent supply and demand factors. In all, we collected data on 26 separate metrics for the period FY10 to FY14. See Table I for the definition of these first 26 variables. While data from recruiting leadership was available at the market level, open source data were collected almost universally at the county level. This presented us with a fundamental difficulty because recruiting market boundaries – defined by a set of ZIP codes – are incompatible with political boundaries.

Because the market level data provided the greatest level of resolution, we devised a method of weighting county-level data to express it in terms of recruiting market boundaries. Let  $Z_i \subseteq Z$  be the subset of (m = 1, 2, 32846) ZIP Code Tabulation Areas (ZCTAs) within each unit *i* boundary. Let *C* be the set of (n = 1, 2, 3141) counties in the USA. Let  $C'_i$  be the set of counties which intersect with a ZCTA in a unit's area of responsibility  $(C'_i \subseteq \{C \cap Z_i\})$ . We then define a weighted statistic *z*<sup>'</sup>, for unit *i* (scripts *j* and *t* are omitted because this definition applies to all variables and times) as:

$$z_i' = \sum_{m \in Z_i} \sum_{n \in C_i'} \nu_{m(n)} z_n \tag{1}$$

where I  $v_{m(n)} \equiv$  the proportion of county *n* population residing in ZCTA *m*, from the 2010 Census and  $Z_n \equiv$  the available discrete statistic for county *n*, where  $|z_n| \ge 1$  (USA Census Bureau, 2015).

We implemented equation (1) only for fractional data, applying [equation (1)] separately to the numerator and the denominator prior to dividing. We explored weighting a raw value such as population but found that aggregating to market levels produced a total value greater than the original. This is likely due to some double-counting in our formulation of  $z_i'$ . However, we assume that similar over-estimation errors applied to the numerator and denominator of a single rate are likely to cancel each other out. The reasonability of our resulting weighted values further increased our confidence in this method.

We also took care to ensure our sample size of time series data were adequate. A common rule of thumb is to have at least 50 observations for model estimation (Montgomery *et al.*, 2015, p. 39). Recruiting data in the model estimation set provided a suitable N = 45 observation. However, much of the county-level data proved available only at annual,

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Index	Variable name	Description	Complex geographical
$\frac{1}{2}$	Voter participation rate Sponsor share	Votes cast for president/total adult population (2008 and 2012, County) Number of Army active duty sponsors/total active duty military	marketing
2	Sponsor share	sponsors (2010-2013, Annual, ZIP code)	areas
3	Labor participation rate	Persons in labor force/total working-age population (2010-2014, Annual, County)	
4	Unemployment rate	Employed persons/persons in labor force (2010-2014, Monthly, County)	73
5	Cohort HS graduation rate	Graduates from freshman high school class/size of freshman class (2010-2014, Annual, County)	
6	Violent crimes	Number of violent crimes (2010-2014, Annual, County)	
7	Obesity	Number of obese persons/total population (2010-2014, Annual, County)	
8	Illicit drug use	Number of persons using illicit drugs/total Population (2010 and 2012, County)	
9	Urban population rate	Number of persons in urban zones/total population (2006 and 2013, County)	
10	Propensity	Number of youth inclined toward military service (2010-2014, Semiannual, Battalion)	
11	QMA population	Number of youth aged 17-24, qualified without a waiver (2010-2014, Annual, ZIP Code)	
12	17-24 Population	Number of youth aged 17-24 (2010-2014, Annual, ZIP Code)	
13	Battalion recruiting station identifier (RSID)	Recruiting battalion boundaries (2010-2014, Annual, ZIP Code)	
14	Lag-1	Number of total contracts produced from previous month (2010-2014, Monthly, Battalion)	
15	Reg. Army GA Mission	Goal for number of GA contracts (2010-2014, Monthly, Battalion)	
16	Reg. Army SA Mission	Goal for number of SA contracts (2010-2014, Monthly, Battalion)	
17	Reg. Army OTH Mission	Goal for number of OTH contracts (2010-2014, Monthly, Battalion)	
18	Reg. Army GA Achieved	Number of adjusted GA contracts produced (2010-2014, Monthly, Battalion)	
19	Reg Army SA Achieved	Number of adjusted SA contracts produced (2010-2014, Monthly, Battalion)	
20	Reg. Army OTH Achieved	Number of adjusted OTH contracts produced (2010-2014, Monthly, Battalion)	
21	Contract share	Number of Army contracts/all DoD contracts (2010-2014, Monthly, Battalion)	
22	Recruiter share	Number of Army recruiters/all DoD recruiters (2010-2014, Monthly, Battalion)	
23	Army recruiters	Number of Army active and reserve recruiters based on PERSTAT (2010-2014, Monthly, Battalion)	
24	Appointments made	Number of appointments scheduled and reported to USAREC (2010- 2014, Monthly, Battalion)	Table I.           Variable names and
25	Appointments conducted	Number of appointments conducted and reported to USAREC (2010- 2014, Monthly, Battalion)	definition of original 26 variables
26	Processing days	Number of days to process recruits (2010-2014, Monthly, Battalion)	considered

semi-annual or quarterly intervals. We therefore expanded the county-level data to that of its recruiting counterpart by applying stochastic mean value imputation to the county data. This involved creating random realizations of monthly county-level data points along a trend-line between the observed annual data (Montgomery *et al.*, 2015, pp. 18-19).

trend-line between the observed annual data (Montgomery *et al.*, 2015, pp. 18-19). To illustrate the imputation, let  $z'_t$  and  $z'_{t+12}$  be realizations of a market-level statistic at the same month *t* in subsequent years; the in-between monthly values of  $z'_{t+2}, z'_{t+3}, \ldots, z'_{t+11}$  must be imputed. We obtain the mean values for all imputed *t*,  $\hat{\mu}_t$ , by subtracting  $z'_t$  from  $z'_{t+12}$  and dividing by 12 to obtain the gradient,  $\delta$  such that  $\hat{\mu}_t = z'_t + \delta t$  for t = 1, 2, 12. JDAL 1,1
A conservative standard deviation  $\hat{\sigma}$  is then  $\hat{\sigma} = (12\delta)/4 = 3\delta$  (Wackerly *et al.*, 2008, pp. 10-11). The parameters  $\hat{\mu}_t$  and  $\hat{\sigma}$  are then used to impute the random realizations for each  $z'_{t+1}, z'_{t+2}, \dots, z'_{t+11}$  by sampling from a normal distribution.

#### Modeling methodology

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A common approach in the past research builds a linear regression or time series model involving numerous potential variables, seemingly without regard to multicollinearity. We used a more rigorous modeling process.

Variables 17-19 in Table I are used as dependent variables with all other variables as potential predictor or independent variables. Principle component analysis provided the basis for the response choice. Principle component analysis is also used to reduce the dimensionality of the predictor set of variables (and thus reducing multicollinearity when using the full set). The reduced set is modeled based on stepwise regression techniques using  $R_{adj}^2$  to judge model fit and studentized residuals to conduct residual analysis when assessing model adequacy. Model adequacy involved residual plots to assess constancy of variance and reasonable normality, whereas measures such as Cook's distance and Hatmatrix elements were used to examine potential outliers or influential points. Details of these analyses are found in McDonald (2016).

Validation of forecasts

#### Data splitting

The primary purpose of our models is to predict future data. Model validation examines how well the estimated model performs in the presence of future data. Data splitting is used to conduct model validation. Observations t = 1, 2, T define the estimation set used in the model building processes, whereas observations  $t = T + 1, T + 2, T + \tau$  define the validation set. In our data set, we let T = 45 and  $\tau = 15$  as 15 to 20 observations are recommended to gain an adequate assessment of prediction performance (Montgomery *et al.*, 2012, p. 375) and recruiting leadership begins setting missions a few months prior to the next full recruiting year. By adding three months to the validation set, we effectively re-create the decision situation from the leadership's point of view, predicting contract production over an extended planning horizon using only the data realized by the forecast origin, T.

#### **Forecast metrics**

The usual metrics of model fit such as  $R_{Adj}^2$  and  $R_{Pred}^2$  do not apply as forecast accuracy metrics. The following two metrics are used for assessing forecasting accuracy:

$$MAD = \frac{1}{N} \sum_{t=T+1}^{T+\tau} \left| y_t - \hat{y}_t \right|$$
$$MAPE = 100\% \cdot \frac{1}{N} \sum_{t=T+1}^{T+\tau} \left| \frac{y_t - \hat{y}_t}{y_t} \right|$$
(2)

where  $y_t$  is the actual response at lead time T + 1, T + 2,  $T + \tau$  and  $\hat{y_t}$  is the predicted value of the same (Montgomery *et al.*, 2015, pp. 64-74). Because the mean absolute deviation is scale-dependent, we also use the mean absolute per cent error.

We assume independent model and variable forecast errors for a one period-ahead forecast, providing a 100 per cent  $(1 - \alpha)$  prediction interval as:

$$100(1 - \alpha)\% \text{ PI} = \hat{y}_{t+1} \pm z_{\alpha/2} \sqrt{\hat{\sigma}_a^2 + \hat{\beta}^2 \hat{\sigma}_x^2}$$
(3)

where  $z_{\alpha/2}$  is the  $(1 - \alpha)$  per cent critical value,  $\hat{\sigma}_a^2$  is the variance estimator regressing  $e_{t-1}$  on  $e_t$ ,  $\hat{\beta}^2$  is the square of the coefficient for *x* obtained from the model and  $\hat{\sigma}_x^2$  is the NID(0,  $\sigma^2$ ) estimate of error variance obtained from the first-order autoregressive model of *x* (Montgomery *et al.*, 2015, pp. 202-204). We generalize the results found in equation (3) for multiple independent regressors to obtain:

$$100(1-\alpha)\%\text{PI} = \hat{y}_{t+1} \pm z_{\alpha/2} \sqrt{\hat{\sigma}_a^2 + \sum_{x_j \in \hat{\mathbf{x}}} \hat{\beta}_j^2 \hat{\sigma}_{x_j}^2}$$
(4)

where we denote the set of forecast regressors with  $\hat{\mathbf{x}}$ .

To implement equation (4) in a predictive role, simple trend models are used to extrapolate independent factors into the future prediction periods.

#### Empirical results

Response and variable determination

The first phase of the work examined the current USAREC modeling approach. The current approach involves a response constructed using some of the data in Table I. Using the variable index indicated in Table I the output response used is:

$$y_1 = \frac{x_{18} + x_{19}}{x_{23}} = f(x_4, x_{10}, x_{13}, x_{27}, x_{28}, x_{29})$$
(5)

where:

$$x_{27} = (x_{15} + x_{16} + x_{17})/x_{23} \tag{6}$$

$$x_{28} = (x_{15} + x_{16})/x_{23} \tag{7}$$

$$x_{29} = (x_{18} + x_{19} + x_{20})/x_{23}.$$
(8)

The current USAREC model is relatively parsimonious and produces a good fit  $(R_{Adj}^2 = 0.93)$ . The model including  $x_{29}$  provides a somewhat better fit. However, it contains a rather concerning issue in its formulation: the predictor  $x_{29}$  is almost identical to the response,  $y_1$ . To improve upon the USAREC approach, we therefore reconsidered how to approach the entire modeling process.

The first step was to reconsider the range of responses available. There are seven potential responses as summarized in Table II. Note the first response comes from the current USAREC approach and the second response is the variable  $x_{29}$  removed from the current model. The other five are responses are found in Table I.

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A principle components analysis was conducted on these responses and revealed loadings on two quantities, one being  $y_4$ . Because responses  $y_1$ ,  $y_2$  and  $y_7$  are all ratio values, all involving the  $x_{19}$  variable, the logical choice was to use responses  $y_3$ ,  $y_4$  and  $y_5$ . These provide meaningful responses for the model development and are easy to understand. We must note that the independent formulation of SA achieve,  $y_4$ , as a response variable constitutes a remarkable departure from the current USAREC model, which lumps SA and GA Achieved ( $y_3$  and  $y_4$ ) together in the same response. Further discussion is devoted to why this is a sensible departure. Nevertheless, subsequent model development focused on each of these three responses, GA, SA and OTH production (i.e. contracts achieved), respectively.

Multiple regression methods using the three responses and the remaining 23 variables from Table I resulted in serious problems with multicollinearity. A principle components analysis was again used this time to reduce the dimensionality of the independent variable set. As Figure 1 indicates, five components account for approximately 79 per cent of the variance. The initial set of loadings are provided in Table III. Using the loadings and factors, along with context knowledge of the problem and a few iterations of principle component analysis, we finalized the set of five component variables as  $x_4$  along with the derived variables:

	Responses	How defined using Table I variables
<b>Table II.</b> Responses considered in re- examination of a casual model for recruitment forecasting	$y_1$ (GSA_PR) $y_2$ (Vol_PR) $y_3$ (GA Achieved) $y_4$ (SA Achieved) $y_5$ (OTH Achieved) $y_6$ (GA + SA Achieved) $y_7$ (Contract Share) Note: Labels for each of the variables used found in Table I	$\begin{array}{c} (x_{18}+x_{19})/x_{23} \\ (x_{18}+x_{19}+x_{20})\!/x_{23} \\ x_{18} \\ x_{19} \\ x_{20} \\ x_{18}+x_{19} \\ x_{21} \end{array}$

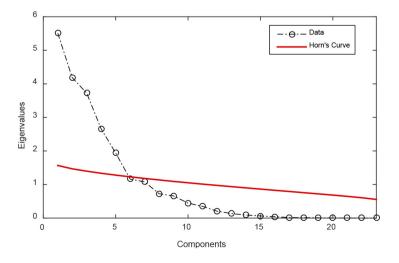


Figure 1. Principal component eigenvalues and Horn's curve for independent variable candidates

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Variable	PC(1)	PC(2)	PC(3)	PC(4)	PC(5)	Complex geographical
$\overline{x_1}$	0.4724	0.6486	-0.0628	-0.0948	0.2746	marketing
$x_2$	0.5045	0.7153	0.0180	0.0579	-0.0407	0
x <sub>3</sub>	-0.7619	0.2076	0.2354	-0.3092	0.2346	areas
$x_4$	-0.0377	-0.4225	-0.6136	-0.0599	0.5270	
<i>x</i> <sub>5</sub>	-0.4288	0.5901	0.4573	0.0041	-0.1782	
$x_6$	-0.0709	-0.2936	-0.7065	-0.3887	0.0780	77
x <sub>7</sub>	0.5014	0.7327	0.0519	0.1881	-0.0123	
<i>x</i> <sub>8</sub>	-0.7177	-0.4122	0.0862	0.1361	0.2085	
<i>x</i> <sub>9</sub>	-0.4932	-0.7896	0.0706	-0.0925	-0.2529	
<i>x</i> <sub>10</sub>	0.6309	-0.4604	-0.2794	0.2299	-0.3635	
<i>x</i> <sub>11</sub>	-0.6595	0.3620	0.2762	-0.4695	0.1842	
<i>x</i> <sub>12</sub>	-0.7745	0.1379	0.3073	-0.4403	0.0694	
x <sub>15</sub>	0.5548	-0.2439	0.2772	-0.4699	0.4496	
<i>x</i> <sub>16</sub>	0.2977	-0.1260	0.7181	0.1922	0.1013	
x <sub>17</sub>	0.7237	-0.2960	-0.0005	-0.2013	0.2052	
$x_{22}$	0.3273	0.1584	-0.2562	-0.6416	-0.0017	
$x_{23}$	0.3109	0.2602	-0.5920	-0.5654	0.0165	
<i>x</i> <sub>24</sub>	0.2679	-0.1399	0.3664	-0.7385	-0.3609	
$x_{25}$	0.3141	-0.2481	0.3994	-0.5156	-0.5592	
<i>x</i> <sub>26</sub>	-0.0334	0.0158	0.0654	0.1292	-0.0716	Table III.
x <sub>27</sub>	0.5856	-0.3851	0.6286	-0.0026	0.3038	
$x_{28}$	0.3848	-0.2956	0.7824	0.0378	0.2950	Principle components analysis summary
Notes: Labe	for initial variable set					
					(0)	
		$x_{30} =$	$x_{25}/x_{24}$		(9)	
					(10)	

$$x_{31} = x_{15} + x_{17} \tag{10}$$

$$x_{32} = x_{10} / x_{23} \tag{11}$$

$$x_{33} = x_{12}x_{10}x_5(1 - x_7) \tag{12}$$

In general terms,  $x_4$  captures unemployment rates,  $x_{30}$  the ratio of appointments (a surrogate for recruiter effort),  $x_{31}$  the combined GA and OTH mission,  $x_{32}$  the SA contracts per recruiter and  $x_{33}$  a measure of the young adults available. This reduction from 23 potential variables to just 5 variables is an important modeling consideration.

To conclude this portion, we provide the final correlation matrix for the five variables selected. Of the ten off-diagonal elements in Table IV, seven are less than |0.2|. We note

Variable	$x_4$	$x_{30}$	<i>x</i> <sub>31</sub>	<i>x</i> <sub>32</sub>	<i>x</i> <sub>33</sub>	
$egin{array}{c} x_4 & & \ x_{30} & & \ x_{31} & & \ x_{32} & & \ x_{33} & & \ \end{array}$	1	-0.213 1 symm	0.196 0.130 1	-0.370 0.199 0.073 1	-0.086 0.409 0.079 0.077 1	Table IV.Correlation matrix Rfor the reduced set ofindependentvariables



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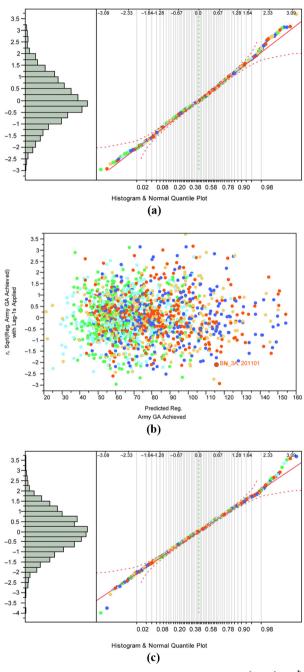
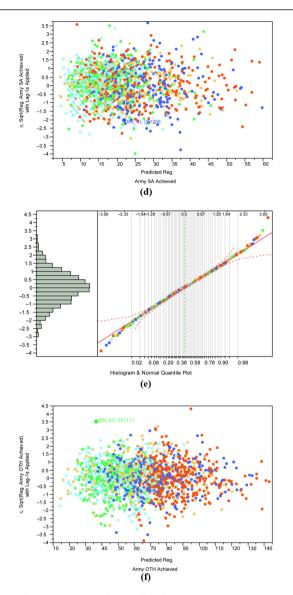
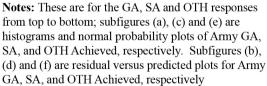


Figure 2.

Left side are quantile plots showing general acceptance of normality assumption. Right side are plots indicating no issues with the constant variance assumption

(continued)





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Figure 2.

**IDAL** entries of 0.37 and 0.41, but these are still both less than 0.5 and are deemed not overly troublesome. Thus, we are confident that this reduced set of five variables are adequate for final model development.

#### Mixed stepwise selection

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Table V.

An initial examination via stepwise regression ruled out quadratic models or linear models with interaction terms. Thus, a pure first-order model is used. Further, based on Box-Cox analyses, all responses were transformed via the square root transformation to improve compliance with the constant variance assumption of the residuals. Despite the transformation, autocorrelation remained present in the residuals. Adding a first-order autoregressive term to the model alleviated this concern. Finally, we needed to model each of the battalions within USAREC. This was done using indicator variables for each market, while simultaneously allowing for the predictor effects to change between markets (i.e. we modeled categorical-continuous interactions). The final models, while seemingly complex, facilitated model adequacy analyses.

Figure 2 provides the pertinent results of the model adequacy analysis. The models for GA, SA and OTH contracts are ordered top to bottom. On the left, we see no reason to doubt reasonable normalcy of the residuals and on the right side we see no reason to doubt the constancy of variance. Residual analysis for outliers and influential points revealed nothing of concern. Table V provides the summary of each model fit. While value of p, the number of terms in the model, is high, the vast majority of these are the indicator variables used to derive the individual battalion models.

Overall, we achieve substantial improvement in terms of model fit -600, 200 and 131 per cent for SA, OTH and GA contract types, respectively - as measured by the estimation data  $R_{Adi}^2$  over the previous effort in (Dertouzos and Garber, 2008). Our improvement comes with some cost of increased *p* although this is a result of our use of more highly specific geographical market areas[1]. We refrain from direct comparisons to other studies, particularly that of Gibson *et al.* (2011) due to incongruities in the types of responses and units of observation used. Final models for each contract type are provided in Tables VI to VIII.

#### Validation forecasts

The real test of any quantitative model is how well it performs out-of-sample. For this study, the most recent 15 time periods of data were held out for validation purposes. Each model was forecast out for these 15 periods at a consolidated level (all contract types and battalions combined) and at a detail level (by contract type). Two prediction interval bands are provided, 80 and 95 per cent as analysts vary in how much risk to assume with respect to the certainty of the input independent variables driving the forecast.

Figure 3 is a comprehensive look across all contract types. Within the model data, the prediction values (dark line) track nicely with the actual data (gray line). Tracking is less

Summary of fit for						
the final transformed, lag-1 models with	Response	$R^2_{Adj}$	$R^2_{Pred}$	$P > F_0$	Þ	Ν
non-significant, non- hereditary terms removed	(Reg. Army GA Achieved) <sup>1/2</sup> (Reg. Army SA Achieved) <sup>1/2</sup> (Reg. Army OTH Achieved) <sup>1/2</sup>	0.740 0.698 0.807	0.730 0.679 0.795	< 0.001 < 0.001 < 0.001	89 100 98	1672 1672 1672

Battalion	Intercept	$oldsymbol{eta}_{x_4}$	$\boldsymbol{\beta}_{x_{30}}$	$oldsymbol{eta}_{x_{31}}$	$\boldsymbol{\beta}_{x_{32}}$	Lag	Complex geographical
BN 1A	6.0013	26.4225	-4.2724	0.0245	-2.0811	0.0028	marketing
BN 1B	3.1563	26.4225	0.8758	0.0245	-2.0811	-0.0010	0
BN 1D	3.5834	26.4225	0.8758	0.0245	-2.0811	-0.0029	areas
BN 1E	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0020	
BN 1G	6.5452	26.4225	-7.4793	0.0245	-2.0811	0.0103	
BN 1K	4.7563	26.4225	0.8758	0.0245	-2.0811	-0.0008	81
BN 1N	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0069	_
BN 10	4.2881	26.4225	0.8758	0.0245	-2.0811	0.0108	
BN 3A	5.6542	26.4225	-3.0809	0.0245	-2.0811	-0.0031	
BN 3D	3.9949	26.4225	0.8758	0.0245	-2.0811	0.0070	
BN 3E	-1.9996	72.9264	0.8758	0.0245	-2.0811	0.0020	
BN 3G	0.8969	26.4225	0.8758	0.0245	-2.0811	0.0106	
BN 3H	0.8771	26.4225	0.8758	0.0245	2.9382	0.0046	
BN 3J	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0058	
BN 3N	0.4258	47.3275	0.8758	0.0245	-2.0811	0.0043	
BN 3T	0.3884	26.4225	0.8758	0.0245	-2.0811	0.0199	
3N 4C	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0069	
3N 4D	1.5753	26.4225	0.8758	0.0358	-2.0811	0.0021	
BN 4E	3.3289	26.4225	0.8758	0.0245	-2.0811	0.0060	
BN 4G	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0087	
BN 4J	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0074	
BN 4K	-1.0958	60.5243	0.8758	0.0245	-2.0811	0.0128	
BN 4P	2.6972	26.4225	0.8758	0.0245	-2.0811	0.0023	
3N 5A	1.3459	26.4225	0.8758	0.0245	-2.0811	0.0094	
BN 5C	4.1218	4.2068	0.8758	0.0245	-2.0811	0.0022	
BN 5D	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0045	
BN 5H	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0060	
BN 5I	-0.0926	41.0251	0.8758	0.0245	-2.0811	0.0069	
BN 5J	1.4253	26.4225	0.8758	0.0245	-2.0811	0.0151	
BN 5K	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0104	
BN 5N*	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0058	
BN 6F	4.947	26.4225	0.8758	0.0245	-2.0811	-0.0054	
BN 6H	2.1978	26.4225	0.8758	0.0245	-2.0811	0.0078	
SN 6I	3.7050	26.4225	0.8758	0.0245	-2.0811	-0.0056	
BN 6J	1.1932	26.4225	0.8758	0.0437	-2.0811	-0.0005	
BN 6K	3.7902	26.4225	0.8758	0.0245	-2.0811	0.0079	
BN 6L	2.4804	26.4225	0.8758	0.0245	-2.0811	0.0089	
SN 6N	3.491	26.4225	3.7986	0.0245	-2.0811	0.0034	Table VI
	0.101	20.1220	0.1500	0.0240	2.0011	0.0004	Final GA models for

accurate in the validation data (as one should suspect) but overall not too bad. Figure 4 breaks this data out in the echelon format by contract type. Figure 5 provides a summary of the validation metrics defined for our effort; again, overall these results are very reasonable. We note with particular satisfaction the prediction intervals obtained using linear trend forecasts of the predictors themselves (i.e. "Unknown *X*"). Only during the very farthest regions of the forecast horizon do we see the actual data e xceed our prediction intervals for both 80 and 90 per cent probability.

We have included the  $R^2$  of each contract type at the aggregate level to compare the estimation models and previous literature for which only Dertouzos and Garber (2008) provide a reliable basis for a comparison; our validation  $R^2$  achieves 530, 170 and 119 per cent relative improvements over the models estimated by Dertouzos and Garber (2008) for

JDAL 1,1	Battalion	Intercept	$oldsymbol{eta}_{x_4}$	$eta_{x_{30}}$	$oldsymbol{eta}_{x_{31}}$	$eta_{x_{32}}$	$oldsymbol{eta}_{x_{33}}$	Lag
1,1	BN 1A	3.7519	15.2018	-0.9503	0.0200	-0.2294	$4.82 \ x \ 10^{-6}$	0.004
	BN 1B	4.8331	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.0009
	BN 1D	3.3435	15.2018	-0.9503	0.0200	-0.2294	$4.82 \ x \ 10^{-6}$	0.014
	BN 1E	3.0128	15.2018	-0.9503	0.0200	-0.2294	$4.82 \ x \ 10^{-6}$	0.018
00	BN 1G	4.8331	15.2018	-0.9503	0.0200	-0.2294	$4.82 \ x \ 10^{-6}$	0.003
82	BN 1K	5.7101	15.2018	-0.9503	0.0200	-0.2294	$-2.26 \ x \ 10^{-5}$	0.014
	BN 1N	3.7381	15.2018	-0.9503	0.0200	-0.2294	$4.82 \ x \ 10^{-6}$	0.004
	BN 10	4.4737	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.019
	BN 3A	4.9531	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.005
	BN 3D	5.6615	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.000
	BN 3E	0.5804	63.6241	-0.9503	0.0200	-0.2294	$3.68 \times 10^{-5}$	0.006
	BN 3G	8.3778	15.2018	-0.9503	0.0200	-0.2294	$-4.67 \times 10^{-5}$	0.001
	BN 3H	4.2080	15.2018	-0.9503	0.0200	3.1698	$4.82 \times 10^{-6}$	0.008
	BN 3J	4.6361	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.009
	BN 3N	0.0017	39.9493	-0.9503	0.0200	-0.2294	$4.95 \times 10^{-5}$	0.001
	BN 3T	8.0054	15.2018	-4.3841	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.002
	BN 4C	4.3254	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.006
	BN 4D	3.4651	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.014
	BN 4E	4.8331	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.000
	BN 4G	3.5428	15.2018	-0.9503	0.0298	-0.2294	$4.82 \times 10^{-6}$	0.000
	BN 4J	4.7788	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.007
	BN 4K	0.5943	64.6082	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.008
	BN 4P	2.7029	50.8070	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.005
	BN 5A	3.4791	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.007
	BN 5C	4.2807	15.2018	-0.9503	0.0211	-0.2294	$4.82 \times 10^{-6}$	0.007
	BN 5D	4.0023	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.006
	BN 5H	6.4252	15.2018	-0.9503	0.0114	-0.2294	$4.82 \times 10^{-6}$	0.015
	BN 5I	4.4255	15.2018	-0.9503	0.0200	-6.0886	$4.82 \times 10^{-6}$	0.007
	BN 5J	3.2492	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.011
	BN 5K	3.3761	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.010
	BN 5N*	4.8331	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	-0.001
	BN 6F	4.313	15.2018	-0.9503	0.0200	-0.2294	$-1.71 \times 10^{-5}$	0.022
	BN 6H	4.2229	15.2018	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.016
	BN 6I	4.8073	15.2018	-0.9503	0.0129	-0.2294	$4.82 \times 10^{-6}$	0.004
	BN 6J	0.9208	40.7777	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.019
	BN 6K	0.6777	50.6793	-0.9503	0.0200	-0.2294	$4.82 \times 10^{-6}$	0.018
Table VII.	BN 6L	4.0834	15.2018	-0.9503	0.0200	-4.1426	$4.82 \times 10^{-6}$	0.016
Final OTH models	BN 6N	0.0084	61.7380	-0.9503	0.0200	-0.2294	$-7.84 \times 10^{-6}$	0.005
for all Battalions	Note: The '	<sup>*</sup> indicates bas	eline					

SA, OTH and GA contract types, respectively. This is a remarkable feat, especially considering the use of forecast inputs for predictor variables in our models.

#### *Comparative analysis*

The causal models developed are based on using multivariate statistical methods to obtain appropriate responses and parsimonious models; these goals were achieved quite well. However, any modeling effort involving many independent variables must answer the question of whether a simpler model would suffice. To this end each model was compared to a naive forecast, an appropriately fit seasonal autoregressive integrated moving average model and a seasonal smoothing method (e.g. the Holt-Winters or Brown's method). Figure 6 plots the

Battalion	QTR 1	QTR 2	QTR 3	QTR 4	ß	ß	β	ß	Lag	Complex
Dattanon	QINI	QIN 2	QINJ	QIN 4	$\beta_{x_4}$	$\beta_{x_{30}}$	$\beta_{x_{31}}$	$\beta_{x_{33}}$	Lag	geographical
BN 1A	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0051	marketing
BN 1B	-2.1747	-1.8306	-1.3374	-2.5265	-12.7345	7.3834	0.0107	$1.47 \ x \ 10^{-6}$	0.0155	0
BN 1D	2.9588	3.3029	3.7961	2.607	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0335	areas
BN 1E	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0004	
BN 1G	1.8122	2.1564	2.2980	1.4604	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0314	
BN 1K	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$8.82 \times 10^{-6}$	0.0314	83
BN 1N	3.6116	3.9557	3.5476	3.8873	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	-0.0053	
BN 10	-2.2302	-1.2794	-1.3929	-2.582	-12.7345	6.8295	0.0107	$1.47 \ x \ 10^{-6}$	0.0185	
BN 3A	9.5942	9.9383	10.4315	9.2424	-69.8499	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	-0.0159	
BN 3D	-1.6317	-1.2875	-0.7943	-1.9835	-12.7345	0.5186	0.0107	$1.30104 \ x \ 10^{-4}$	-0.0065	
BN 3E	0.6327	0.9769	1.4701	0.2809	-12.7345	5.3432	0.0107	$1.47 \ x \ 10^{-6}$	0.0126	
BN 3G	3.7872	4.1313	4.6245	3.4354	-12.7345	0.5186	0.0023	$1.47 \ x \ 10^{-6}$	0.0179	
BN 3H	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0021	
BN 3J	6.9493	7.2935	7.7866	6.5975	-44.7603	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0015	
BN 3N	1.9630	2.3071	2.8003	0.9800	-12.7345	4.6567	0.0107	$1.47 \ x \ 10^{-6}$	0.0032	
BN 3T	3.4437	3.7878	4.281	3.0919	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	-0.0221	
BN 4C	8.1182	8.4624	8.9555	7.7664	-12.7345	-4.5569	0.0107	$1.47 \ x \ 10^{-6}$	-0.0141	
BN 4D	6.8775	7.2216	7.7148	6.5257	-49.211	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	-0.0095	
BN 4E	3.4288	3.773	4.2662	2.5276	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0082	
BN 4G	3.7728	4.1170	4.6102	3.4210	-12.7345	0.5186	0.0107	$1.47 \times 10^{-6}$	-0.0131	
BN 4J	3.6719	3.4995	4.5093	3.3201	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0076	
BN 4K	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	0.0037	
BN 4P	6.3981	6.2528	7.2354	6.0463	-25.392	0.5186	0.0107	$1.47 \times 10^{-6}$	-0.0248	
BN 5A	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \ x \ 10^{-6}$	-0.0126	
BN 5C	5.6229	5.9670	6.4602	5.2711	-12.7345	-2.6684	0.0107	$1.47 \ x \ 10^{-6}$	0.0042	
BN 5D	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \times 10^{-6}$	-0.0052	
BN 5H	2.9113	3.2555	3.7487	2.5595	-12.7345	0.5186	0.0192	$1.47 \times 10^{-6}$	0.0128	
BN 5I	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \times 10^{-6}$	0.0008	
BN 5J	6.2880	6.6322	7.1253	5.9362	-12.7345	-3.0345	0.0107	$1.47 \times 10^{-6}$	0.0180	
BN 5K	3.0773	3.0012	3.9147	2.7255	-12.7345	0.5186	0.0107	$1.35 \times 10^{-5}$	0.0042	
BN 5N*	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \times 10^{-6}$	0.003	
BN 6F	3.2325	3.5766	4.0698	2.8806	-12.7345	0.5186	0.0107	$1.47 \times 10^{-6}$	-0.0046	
BN 6H	3.6321	3.9763	4.4695	3.2803	-12.7345	0.5186	0.0107	$-1.01 \times 10^{-5}$	0.0137	
BN 6I	3.5007	3.8449	4.338	3.1489	-12.7345	0.5186	0.0160	$1.47 \times 10^{-6}$	0.0061	
BN 6J	0.2422	0.5864	1.0795	-0.1096	26.5042	0.5186	0.0107	$1.47 \times 10^{-6}$	0.0145	
BN 6K	3.6321	3.9763	4.4695	3.2803	-12.7345	2.642	0.0107	$-1.01 \times 10^{-5}$	0.0145	
BN 6L	3.5736	3.9177	4.4109	3.2218	-12.7345	0.5186	0.0107	$1.47 \times 10^{-6}$	0.0209	Table VIII.
BN 6N	2.6417	2.9858	3.479	2.2899	15.0886	0.5186	0.0107	$-2.53 x  10^{-5}$	-0.0131	
										Final SA models for

Note: The \* indicates baseline

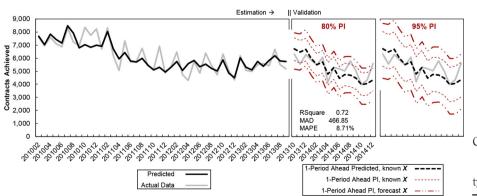
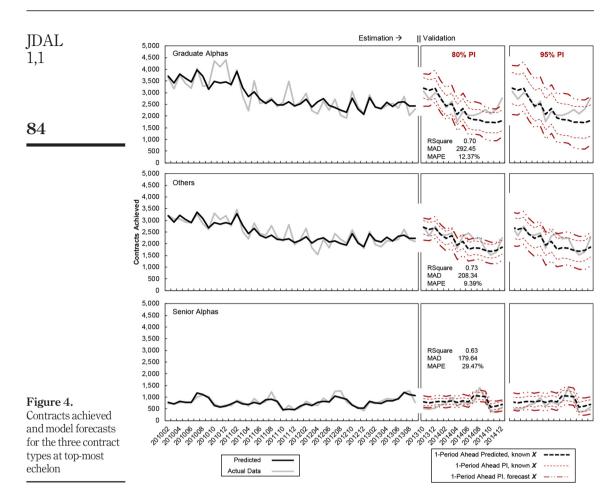


Figure 3. Contracts achieved and model forecast for the total of all contract types, top-most echelon

all Battalions



results for each of the output measures. The legend in each of the sub-figures provide a specification of the univariate model fit; development details are not provided here.

For each of the GA and OTH models, it is quite clear the multivariate models are the preferred approach, realizing of course that these models do already contain a single autoregressive term. For the more seasonal SA response model, the results were not so conclusive as the seasonal time series modeling approaches are comparable options. Overall,

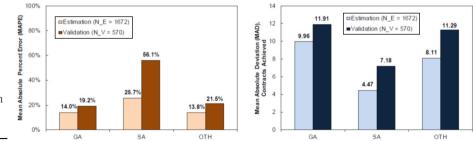
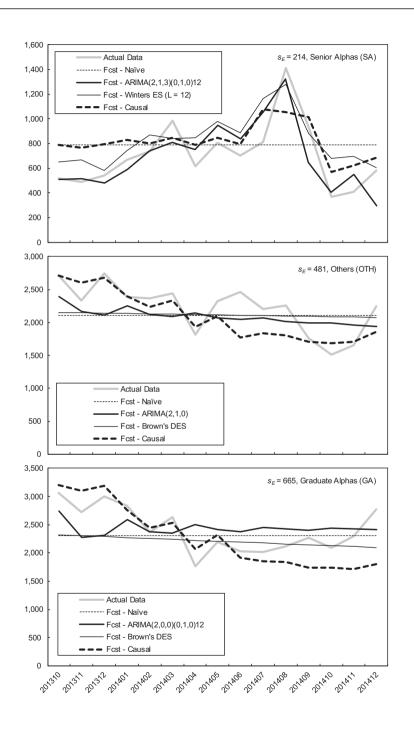


Figure 5. Summary of model validation metrics on the model and holdout data sets



Complex geographical marketing areas



Figure 6. Forecasts of contracts achieved, validation data

JDAL the collective result is that our effort to develop multivariate models is indeed rewarded with improved performance.

#### Conclusion

We have shown, through the use of multiple linear regression aided by increased geographic data specificity through the use of our ZCTA method, mixed stepwise selection methods and PCA, that improvements over previous efforts to model US Army enlistment contract production are possible. Moreover, we have shown that forecasts produced by the multiple linear regression models – which themselves require simple linear forecasts of the predictors – are robust for a relevant forecast horizon of up to 15 months. Indeed, the fit of the forecasts alone constitute remarkable improvements over previous models which did not use validation data and are worth the development effort when compared to simple time series models.

In closing, we must note the unique ability of the multiple regression model in forecasting to consider the effect of inputs which are controlled to a degree by the decision-maker. While the regression model coefficients and standard errors are indeed based only on past data, our models indicated rather high statistical significance of future "controllable" inputs such as recruiting goals and these inputs should be likewise considered in a futuristic sense when the firm is producing forecasts. Only a causal model such as the one afforded by lagged multiple regression affords such an opportunity for exploration. We hope to have successfully informed subsequent discussions on behalf of such a method.

#### Note

1. Dertouzos and Garber (2008) used 68 variables for each contract type, whereas we used 100, 98 and 89 for SA, OTH and GA models, respectively.

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